

# Integrated Scheduling of Multiple System Resources

**Prashant Pradhan**  
**State University of New York,**  
**Stony Brook**

## Motivation

- 1 **Servers in an internet services infrastructure**
  - Each server shared by many principals
  - Each principal requires a performance guarantee (and pays for it)
- 1 **Characteristics of a principal's task :**
  - Requires multiple resources (CPU, link, disk, memory)
  - Has a single, *global* performance requirement

# Motivation

## 1 Example :

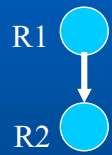
- Periodic task :  
Disk->CPU->Link, Disk->CPU->Link ....
- Work required from each resource :  
100 bytes to be read from disk, 1000 cycles to process data, 100 bits to be sent on the network
- Performance requirement :  
1000 requests/sec

# Motivation

## 1 Only the system has complete knowledge of the performance requirements of all principals

- *Hence the system must translate global performance requirements to per-resource allocations optimally (maximize the number of principals admitted)*

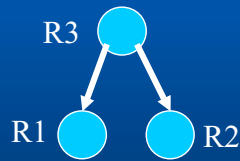
## Resource Usage Topologies



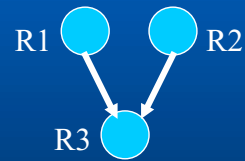
2-series



3-series



Fan-out



Fan-in

## Single Resource Scheduling

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  - Schedulability condition by Figueira and Pasquale

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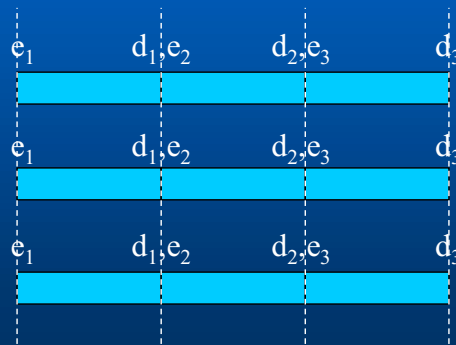
# Single Resource Scheduling

- 1 **RMS : optimal static priority algorithm**
  - Analysed by Liu and Layland

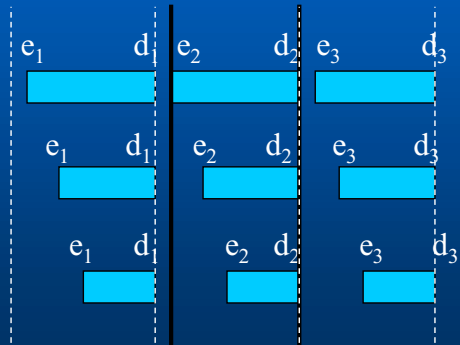
## Key Ideas

- 1 Using an optimal scheduling algorithm in R1 is sufficient but not necessary to schedule the task set
  - use this freedom to optimize admission control in R2
- 1 The key to performing tight admission control in R2 is to accurately characterize the time a task spends waiting in R1
  - determines eligibility in R2

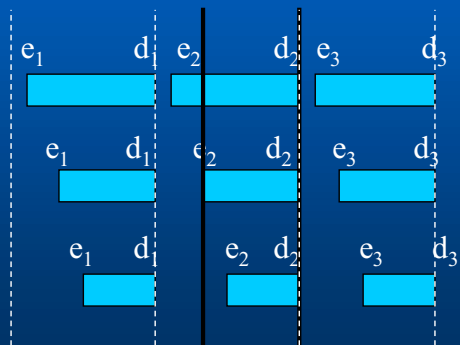
## Key Ideas



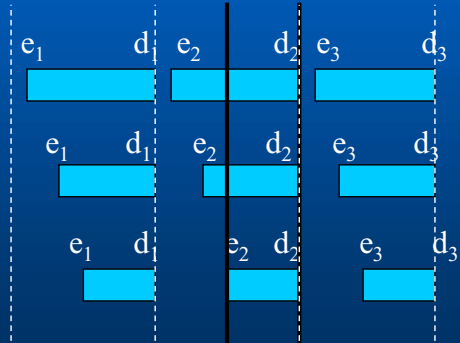
# Key Ideas



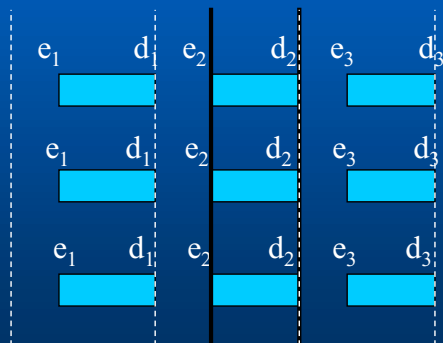
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## Our Approach

### 1 Static priority in R1, EDF in R2

- accurately characterizes the waiting time in R1
- dynamic priority must take into account the pending work in the two resources *at run time*

## Scheduling R1

### 1 Admission control in R2 requires :

$$W1/d1 + W2/d2 + \dots \leq C2$$

### 1 The denominator of a task's term must be reduced by its waiting time in R1

- minimize left hand side

### 1 Pick tasks one-by-one : the next one picked is the one that causes that largest incremental increase in the left hand side



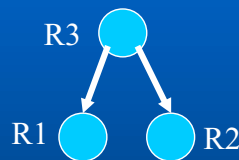
# Scheduling R1

- 1 Now we have two priority orderings for R1 :
  - O1 : RMS
  - O2 : computed to optimize R2
- 1 Calculate a final ordering for R1
  - pick a task from O2 if it does not violate any deadlines in R1
  - if it does, pick a task from O1
  - using the newly picked task, check for admission control in R2
  - till all tasks are admitted

# Extending to Other Topologies



Consider R2 and R3 as one resource. Their final ordering becomes O2 for the 3-series



While picking the ordering O2, normalize the sensitivity of a task by the capacity of its resource

## Deadline Splitting

- 1 A task's deadline  $d$  is split into two pieces  $d_1$  and  $d_2$
- 1 EDF is performed in each resource
- 1 The optimization criterion is to balance the utilization of all resources
  - allocate more relaxed deadline to a heavily utilized resource
- 1 Problem : lack of tight admission control

## Ongoing Work

- 1 Optimality
- 1 Backtracking
- 1 Including memory as a resource

## References

- 1 Figueira N.R. and Pasquale J.; "A Schedulability Condition for Deadline-Ordered Service Disciplines", IEEE/ACM Transactions on Networking, Vol.5, No.2, April 1997.
- 1 Liu C.L. and Layland J.W.; "Scheduling Algorithms for Multiprogramming in a Hard Real-Time Environment", Journal of the ACM, Vol.20, No.1, January 1973, pp. 46-61.
- 1 Chiueh T. and Gopalan K.; "Integrated Real-Time Resource Scheduling", ECSL Technical Report No. 56 (available from [www.ecsl.cs.sunysb.edu/tr/TR56.ps.gz](http://www.ecsl.cs.sunysb.edu/tr/TR56.ps.gz)).